

Topic : Atomic Structure
Type of Questions

Type of Questions	M.M., Min.
Single choice Objective ('-1' negative marking) Q.1 to Q.3	(3 marks, 3 min.) [9, 9]
Multiple choice objective ('-1' negative marking) Q.4	(4 marks, 4 min.) [4, 4]
Subjective Questions ('-1' negative marking) Q.5,6,8,9	(4 marks, 5 min.) [16, 20]
Match the Following (no negative marking) (2 × 4) Q.7	(8 marks, 10 min.) [8, 10]

- If numerical value of mass and velocity are equal for a particle, then its de-Broglie wavelength in terms of K.E. is :
 (A) $\frac{mh}{2K.E.}$ (B) $\frac{h}{2mK.E.}$ (C) both are correct (D) none is correct.
- A wavelength of 400 nm of electromagnetic radiation corresponds to :
 (A) frequency (ν) = 7.5×10^{14} Hz (B) wave number ($\bar{\nu}$) = 2.5×10^6 m⁻¹.
 (C) momentum of photon = 1.66×10^{-27} kg ms⁻¹ (D) all are correct values.
- In one experiment, a proton having initial kinetic energy of 1 eV is accelerated through a potential difference of 3 V. In another experiment, an α -particle having initial kinetic energy 20 eV is retarded by a potential difference of 2 V. The ratio of de-Broglie wavelengths of proton and α -particle is :
 (A) $2\sqrt{6} : 1$ (B) 8 : 1 (C) 4 : 1 (D) $2\sqrt{2} : 1$
- * When photons of energy 4.25 eV strike the surface of a metal A, the ejected photoelectrons have maximum kinetic energy (K.E)_A and de-Broglie wavelength is λ_A . The maximum kinetic energy of photoelectrons liberated from another metal B by photons of energy 4.7 eV is (KE)_B, where (KE)_B = (KE)_A - 1.5 eV. If the de-Broglie wavelength of these photoelectrons is λ_B (= $2\lambda_A$), then :
 (A) The work function of metal A is 2.25 eV (B) The work function of metal B is 4.20 eV
 (C) (KE)_A = 2 eV (D) (KE)_B = 2.75 eV
- Average life time of an electron in hydrogen atom excited to n = 2 state is 10⁻⁸ s. Find the number of revolutions made by the electron on the average, before it jumps to the ground state.
- The ionisation energy of He⁺ ion is 19.6×10^{-18} J per ion. Calculate the energy of the first stationary state of Li²⁺ ion.
- Match the following :**

Column (I)	Column (II)
(A) Binding energy of 5 th excited state of Li ²⁺ sample	(p) 10.2 V
(B) 1 st excitation potential of H-atom	(q) 3.4 eV
(C) 2 nd excitation potential of He ⁺ ion	(r) 13.6 eV
(D) I.E. of H-atom	(s) 48.4 V
- The IP of H-atom is 13.6 V. It is exposed to electromagnetic waves of wavelength 1026 Å and then, it gives out induced radiations. Find the wavelength of all possible induced radiations.
- The ionization energy of a Hydrogen like species is 4 Rydberg. What is the radius of the first orbit of this atom ? (Given : Bohr radius of hydrogen = 5.3×10^{-11} m; 1 Rydberg = 2.2×10^{-18} J)



Answer Key

DPP No. # 16

1. (A) 2. (D) 3. (C) 4.* (A,B,C)
 5. 8.2×10^6 6. -4.41×10^{-17} J. 7. [A - q] ; [B - p] ; [C - s] ; [D - r].
 8. I induced = 1026 Å , II induced = 1216 Å, III induced = 6568 Å 9. 2.65×10^{-11} m.

Hints & Solutions

DPP No. # 16

1. $\lambda = \frac{h}{p} = \frac{h}{mv} = \frac{h}{\sqrt{2KE}}$
 but $v^2 = \frac{2KE}{m}$ therefore $\lambda = \frac{hm}{\sqrt{2KE}}$
2. Use $C = v\lambda$ \Rightarrow $\bar{u} = \frac{1}{\lambda}$
3. $K.E._{\text{proton}} = 1 + (1)(3) = 4 \text{ eV} \therefore \lambda_p = \frac{h}{\sqrt{2m_p(K.E)_p}}$ & $K.E._{\alpha\text{-particle}} = 20 - (2)(2) = 16 \text{ eV} \therefore \lambda_\alpha = \frac{h}{\sqrt{2m_\alpha(K.E)_\alpha}}$
 $\therefore \frac{\lambda_p}{\lambda_\alpha} = \sqrt{\frac{m_\alpha(K.E)_\alpha}{m_p(K.E)_p}} = \sqrt{\frac{4 \times 16}{1 \times 4}} = \frac{4}{1}$
- 4.* $4.25 = (W_0)_A + (K.E.)_A$
 $4.70 = (W_0)_B + (K.E.)_A - 1.5$
 So $(W_0)_B - (W_0)_A = 0.45 + 1.5$
 $= 1.95$
 Now, $\lambda_B = 2\lambda_A$
 $\frac{h}{\sqrt{2m(K.E)_B}} = \frac{2h}{\sqrt{2m(K.E)_A}}$
 So $(K.E.)_A = 4(K.E.)_B$
 $4.25 - (W_0)_A = 4[4.7 - (W_0)_B]$
 $4(W_0)_B - (W_0)_A = 14.55$
 So $(W_0)_B = 4.2 \text{ eV}$
 So $(W_0)_A = 2.25 \text{ eV}$
 $(K.E.)_A = 2 \text{ eV}$
 $(K.E.)_B = 0.5 \text{ eV}$



5. number of revolutions per second

$$= \frac{v}{2\pi r} = \frac{2.18 \times 10^6 \left(\frac{Z}{n}\right)}{2 \times 3.14 \times 0.529 \times \left(\frac{n^2}{Z}\right) \times 10^{-10}} = \frac{2.18 \times 10^6 \left(\frac{1}{2}\right)}{2 \times 3.14 \times 0.529 \times \left(\frac{2^2}{1}\right) \times 10^{-10}}$$

$$\text{Number of revolution in } 10^{-8} \text{ second} = \frac{2.18 \times 10^6 \left(\frac{1}{2}\right)}{2 \times 3.14 \times 0.529 \times \left(\frac{2^2}{1}\right) \times 10^{-10}} \times 10^{-8} = 8.2 \times 10^6.$$

6. The ionisation energy of He^+ is $19.6 \times 10^{-18} \text{ J}$.

$$\therefore \text{Energy of the first orbit of } \text{He}^+ (Z = 2) = 19.6 \times 10^{-18} \text{ J.}$$

$$\therefore \text{Energy of the first orbit of } \text{H}^+ (Z = 1) = \frac{19.6 \times 10^{-18}}{4} \text{ J}$$

$$\therefore \text{Energy of the first orbit of } \text{Li}^{2+} (Z = 3) = \frac{19.6 \times 10^{-18}}{4} \times 9 = 4.41 \times 10^{-17} \text{ J.}$$

7. (A) Transition $n \infty$ to $n \infty$ For Li^{2+} sample

(B) Transition $n \rightarrow 1$ to $n \rightarrow 2$ For H-atom sample

(C) Transition $n \rightarrow 1$ to $n \rightarrow 3$ For He^+ sample

(D) Transition $n \rightarrow 1$ to $n \rightarrow \infty$ For H-atom sample

8. $\Delta E = \frac{12400}{1026} = 12.09 \text{ eV.}$

So, $\Delta E = E_3 - E_1.$

Hence, induced radiations will be correspond to following energy transition

$E_3 \rightarrow E_1, E_3 \rightarrow E_2$ and $E_2 \rightarrow E_1.$

9. $-13.6 \frac{Z^2}{n^2} = 4R = 4 \times 2.2 \times 10^{-18} \text{ J.}$

$$Z^2 = \frac{4 \times 2.2 \times 10^{-18} \text{ J}}{13.6 \times 1.6 \times 10^{-19}} = 4 ; \quad Z = 2.$$

$$r = 0.529 \frac{n^2}{Z} \times 10^{-10} \text{ m.} \quad r = 0.529 \times 10^{-10} \times \frac{1}{2} = 2.645 \times 10^{-11} \text{ m.}$$

